

A is a type of probability experiment with the following characteristics

- 1 There are only two possible outcomes, which can be labeled as success or failure**
- 2 There are a fixed number of trials**
- 3 Each trial is independent**
- 4 The probability of a success is the same on each trial**

n- the number of trials of the experiment

p- the probability of success

q- the probability of failure

x- the number of successes we wish to observe

NOTE: $q = 1 - p$

Suppose we have three randomly selected students who want to enroll at Clemson University. If 54% of all applicants are accepted to Clemson what is the probability that...

- 1 All three of the applicants are accepted?**
- 2 None of the three are accepted?**
- 3 Exactly one of the three are accepted?**
- 4 Exactly two of the three are accepted?**

First, what are all the possible outcomes?

The probability of x successes in n trials of a binomial experiment with probability of success p is

$$P(x) = {}_n C_x \cdot p^x \cdot q^{n-x}$$

The calculator has built-in functions to calculate these probabilities, so you don't need to worry about remembering this formula

A binomial distribution is a type of discrete probability distribution where each value of the random variable is listed, together with its associated binomial probability.

(Ex) Create a binomial distribution for the three students who want to be admitted to Clemson

(Ex) What is the mean and standard deviation of this distribution?

(Ex) Create a cumulative binomial distribution for this example

$$\mu =$$

$$\sigma = \sqrt{npq}$$

The calculator can be used to calculate binomial probabilities using the functions

- 1 $\text{binompdf}(n, p, x)$ - calculates the probability of exactly x successes $P(X = x)$
- 2 $\text{binomcdf}(n, p, x)$ - calculates the probability of at most x successes $P(X \leq x)$

In order to answer questions involving the probability of at least x successes, or more than x successes, or other similar language, you have to learn how to properly manipulate binomcdf in order to do so

Some hints that can help you out are, if the probability you want asks for:

- 1 exactly x successes - use $\text{binompdf}(n, p, x)$
- 2 no more than or less than or equal to x successes - use $\text{binomcdf}(n, p, x)$
- 3 fewer than or less than x successes - use $\text{binomcdf}(n, p, x - 1)$
- 4 more than or greater than x successes - use $1 - \text{binomcdf}(n, p, x)$
- 5 at least x successes - use $1 - \text{binomcdf}(n, p, x - 1)$

You can find these functions by going to the distribution menu: press [2nd] [VARS].

In addition, the app https://david628.github.io/applets/stats/binomial_distribution.html, can be used to help visualize the calculation of binomial probabilities

1 The probability that a person is left handed is 10%. If 15 people are asked, what is the probability that exactly five are left handed?

2 The probability that a household owns a personal computer is 45%. If 20 households are surveyed, what is the probability that exactly 10 have a personal computer?

3 Sixty-five percent of the population has brown eyes. If 8 people are chosen at random, what is the probability that fewer than 3 of them have brown eyes?

